Chapter 11

The Circle of Fifths¹

11.1 Related Keys

The circle of fifths is a way to arrange keys to show how closely they are related to each other.

 $^{^{1}} This\ content\ is\ available\ online\ at\ < http://cnx.org/content/m10865/2.17/>.$

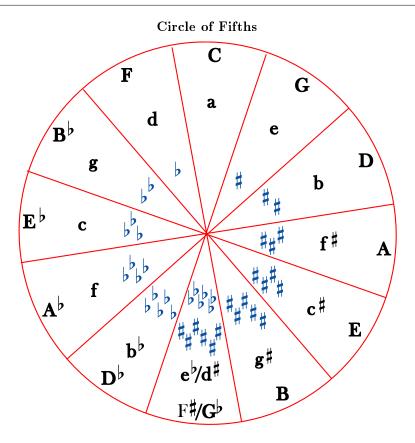


Figure 11.1: The major key for each key signature is shown as a capital letter; the minor key as a small letter. In theory, one could continue around the circle adding flats or sharps (so that B major is also C flat major, with seven flats, E major is also F flat major, with 6 flats and a double flat, and so on), but in practice such key signatures are very rare.

Keys are not considered closely related to each other if they are near each other in the chromatic scale² (or on a keyboard). What makes two keys "closely related" is having similar key signatures (Chapter 7). So the most closely related key to C major, for example, is A minor, since they have the same key signature (no sharps and no flats). This puts them in the same "slice" of the circle. The next most closely related keys to C major would be G major (or E minor), with one sharp, and F major (or D minor), with only one flat. The keys that are most distant from C major, with six sharps or six flats, are on the opposite side of the circle.

The circle of fifths gets its name from the fact that as you go from one section of the circle to the next, you are going up or down by an interval³ of a perfect fifth⁴. If you go up a perfect fifth (clockwise in the circle), you get the key that has one more sharp or one less flat; if you go down a perfect fifth (counterclockwise), you get the key that has one more flat or one less sharp. Since going down by a perfect fifth is the same as going up by a perfect fourth⁵, the counterclockwise direction is sometimes referred to as a "circle of fourths".

 $^{^2}$ "Half Steps and Whole Steps" $<\!$ http://cnx.org/content/m10866/latest/#p0bb>

 $^{^3}$ "Interval" http://cnx.org/content/m10867/latest/

⁴"Interval": Section Perfect Intervals http://cnx.org/content/m10867/latest/#s21

 $^{^5}$ "Interval" <http://cnx.org/content/m10867/latest/#p21b>

(Please review inverted intervals⁶ if this is confusing.)

Example 11.1

The key of D major has two sharps. Using the circle of fifths, we find that the most closely related major keys (one in each direction) are G major, with only one sharp, and A major, with three sharps. The relative minors of all of these keys (B minor, E minor, and F sharp minor) are also closely related to D major.

Exercise 11.1 (Solution on p. 63.)

What are the keys most closely related to E flat major? To A minor?

Exercise 11.2 (Solution on p. 63.)

Name the major and minor keys for each key signature.



Figure 11.2

11.2 Key Signatures

If you do not know the order of the sharps and flats, you can also use the circle of fifths to find these. The first sharp in a key signature is always F sharp; the second sharp in a key signature is always (a perfect fifth away) C sharp; the third is always G sharp, and so on, all the way to B sharp.

The first flat in a key signature is always B flat (the same as the last sharp); the second is always E flat, and so on, all the way to F flat. Notice that, just as with the key signatures, you add sharps or subtract flats as you go clockwise around the circle, and add flats or subtract sharps as you go counterclockwise.

^{6&}quot;Interval": Section Inverting Intervals http://cnx.org/content/m10867/latest/#s3

Add sharps \mathbf{C} in this order \mathbf{F} G 2nd sharp 6th flat 1st sharp 3rd sharp 7th flat 5th flat D 4th sharp 4th flat 5th sharp Α 3rd flat 6th sharp 2nd flat \mathbf{E} 7th sharp 1st flat B Add flats in this order

Adding Sharps and Flats to the Key Signature

Figure 11.3: Each sharp and flat that is added to a key signature is also a perfect fifth away from the last sharp or flat that was added.

Exercise 11.3 (Solution on p. 63.)

Figure 11.1 (Circle of Fifths) shows that D major has 2 sharps; Figure 11.3 (Adding Sharps and Flats to the Key Signature) shows that they are F sharp and C sharp. After D major, name the next four sharp keys, and name the sharp that is added with each key.

Exercise 11.4 (Solution on p. 63.)

E minor is the first sharp minor key; the first sharp added in both major and minor keys is always F sharp. Name the next three sharp minor keys, and the sharp that is added in each key.

Exercise 11.5 (Solution on p. 64.)

After B flat major, name the next four flat keys, and name the flat that is added with each key.

Solutions to Exercises in Chapter 11

Solution to Exercise 11.1 (p. 61)

E flat major (3 flats):

- B flat major (2 flats)
- A flat major (4 flats)
- C minor (3 flats)
- G minor (2 flats)
- F minor (4 flats)

A minor (no sharps or flats):

- E minor (1 sharp)
- D minor (1 flat)
- C major (no sharps or flats)
- G major (1 sharp)
- F major (1 flat)

Solution to Exercise 11.2 (p. 61)

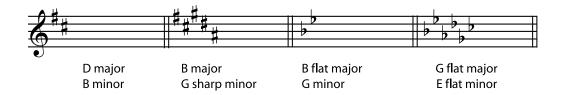


Figure 11.4

Solution to Exercise 11.3 (p. 62)

- A major adds G sharp
- E major adds D sharp
- B major adds A sharp
- F sharp major adds E sharp



Figure 11.5

Solution to Exercise 11.4 (p. 62)

• B minor adds C sharp

- F sharp minor adds G sharp
- C sharp minor adds D sharp



Figure 11.6

Solution to Exercise 11.5 (p. 62)

- E flat major adds A flat
- A flat major adds D flat
- D flat major adds G flat
- G flat major adds C flat



Figure 11.7

INDEX 65

Index of Keywords and Terms

Keywords are listed by the section with that keyword (page numbers are in parentheses). Keywords do not necessarily appear in the text of the page. They are merely associated with that section. Ex. apples, § 1.1 (1) **Terms** are referenced by the page they appear on. Ex. apples, 1

```
A accidentals, 27
                                                           M major, § 7(35)
                                                               major keys, § 8(41), § 11(59)
B bass clef, § 2(7), 7
                                                               major scales, § 8(41)
                                                               mediant, \S 9(47)
C C clef, § 2(7), 9
                                                               minor, \S 7(35)
    chromatic, \S 5(29)
                                                               minor keys, § 11(59)
    clef, \S 1(1), \S 2(7)
                                                               music, § 1(1), § 2(7), § 4(25), § 5(29), § 7(35),
    clef symbol, 7
                                                               \S 9(47)
\mathbf{D} degree, § 9(47)
                                                           N natural, \S 4(25), 25
    diatonic, \S 5(29)
                                                               notation, \S 1(1), \S 2(7), \S 3(19), \S 4(25),
    dominant, \S 9(47)
                                                                \S 7(35)
    double flat, 28
                                                               note, § 1(1)
    double sharp, 28
                                                           O octave, § 6(33)
E enharmonic, \S 4(25), \S 10(51), 52
    enharmonic keys, 54
                                                           P piano, § 3(19)
    enharmonic spelling, 52
                                                               pitch, § 1(1), § 4(25), 25, § 6(33)
F F clef, 10
                                                           \mathbf{R} related keys, § 11(59)
    fifths, § 11(59)
                                                           S scale, 41, § 9(47)
    flat, § 4(25), § 7(35)
    flat sign, 26
                                                               scales, § 8(41)
    flats, § 10(51), § 11(59)
                                                               sharp, \S 4(25), \S 7(35)
                                                               sharp sign, 26
G G clef, 10
                                                               sharps, § 10(51), § 11(59)
                                                               solfege, § 1(1)
H half, \S 5(29)
                                                               staff, § 1(1), § 2(7), § 4(25), § 7(35)
                                                               step, \S 5(29)
\mathbf{K} key, § 7(35), 41, § 10(51)
                                                               subdominant, § 9(47)
    key signature, § 7(35), 35, 43, § 10(51),
                                                               submediant, \S 9(47)
    § 11(59)
                                                               supertonic, \S 9(47)
    keyboard, § 3(19)
    keys, § 8(41)
                                                           {f T} tonal center, 42
                                                               tonic, 42, § 9(47)
L leading, \S 9(47)
                                                               treble, § 2(7)
    ledger, \S 1(1)
                                                               treble clef, § 2(7), 7
    line, \S 1(1)
                                                           \mathbf{W} whole, § 5(29)
```

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